

RDF y SPARQL: Dos componentes básicos para la Web de datos

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“The Semantic Web is an extension of the current web in which information is given well-defined meaning, better enabling computers and people to work in cooperation.”

[Tim Berners-Lee et al. 2001.]

Specific goals:

- ▶ Build a description language with standard semantics
 - ▶ Make semantics machine-processable and understandable
- ▶ Incorporate logical infrastructure to reason about resources
- ▶ W3C proposals: **Resource Description Framework (RDF) and SPARQL**

RDF in a nutshell

RDF is the framework proposed by the W3C to represent information in the Web:

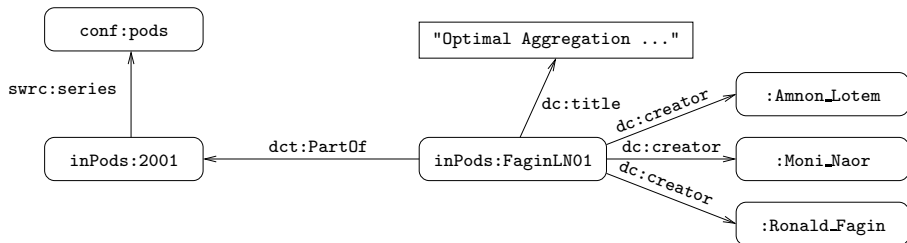
- ▶ URI vocabulary
 - ▶ A URI is an atomic piece of data, and it identifies an abstract resource
- ▶ Syntax based on directed labeled graphs
 - ▶ URIs are used as node labels and edge labels
- ▶ Schema definition language (**RDFS**): Define new vocabulary
 - ▶ Typing, inheritance of classes and properties, ...
- ▶ Formal semantics

An example of an RDF graph: DBLP

```

: <http://dblp.13s.de/d2r/resource/authors/>
conf: <http://dblp.13s.de/d2r/resource/conferences/>
inPods: <http://dblp.13s.de/d2r/resource/publications/conf/pods/>
swrc: <http://swrc.ontoware.org/ontology#>
dc: <http://purl.org/dc/elements/1.1/>
dct: <http://purl.org/dc/terms/>

```



An example of a URI

`http://dblp.l3s.de/d2r/resource/conferences/pods`



PODS | D2R Server publishing the

http://dblp.l3s.de/d2r/page/conferences/pods

Resource URI: http://

[Home](#) | [Example Conferences](#)

Property	Value
<code>rdfs:label</code>	PODS (xsd:string)
<code>rdfs:seeAlso</code>	<code><http://dblp.l3s.de/Venues/PODS></code>
<code>is swrc:series of</code>	<code><http://dblp.l3s.de/d2r/resource/publications/conf/pods/00></code>
<code>is swrc:series of</code>	<code><http://dblp.l3s.de/d2r/resource/publications/conf/pods/2001></code>
<code>is swrc:series of</code>	<code><http://dblp.l3s.de/d2r/resource/publications/conf/pods/2002></code>
<code>is swrc:series of</code>	<code><http://dblp.l3s.de/d2r/resource/publications/conf/pods/2003></code>
<code>is swrc:series of</code>	<code><http://dblp.l3s.de/d2r/resource/publications/conf/pods/2004></code>
<code>is swrc:series of</code>	<code><http://dblp.l3s.de/d2r/resource/publications/conf/pods/2005></code>

URI can be used for any abstract resource

http://dblp.l3s.de/d2r/page/authors/Ronald_Fagin



Ronald Fagin | D2R Server publishing the

Resource URI: http://dblp.l3s.de/d2r/page/authors/Ronald_Fagin

[Home](#) | [Example Authors](#)

Property	Value
is dc:creator of	http://dblp.l3s.de/d2r/resource/publications/conf/aaai/FagiHV86
is dc:creator of	http://dblp.l3s.de/d2r/resource/publications/conf/aaai/FaginHNV94
is dc:creator of	http://dblp.l3s.de/d2r/resource/publications/conf/aaai/HalpernF90
is dc:creator of	http://dblp.l3s.de/d2r/resource/publications/conf/apccm/Fagin09
is dc:creator of	http://dblp.l3s.de/d2r/resource/publications/conf/birthday/FaginHHMPV09
is dc:creator of	http://dblp.l3s.de/d2r/resource/publications/conf/caap/Fagin83
is dc:creator of	http://dblp.l3s.de/d2r/resource/publications/conf/coco/FaginSV93
is dc:creator of	http://dblp.l3s.de/d2r/resource/publications/conf/concur/HalpernF88

Why is this an interesting problem? Why is it challenging?

- ▶ RDF graphs can be interconnected
 - ▶ URIs should be dereferenceable
- ▶ Semantics of RDF is open world
 - ▶ RDF graphs are inherently incomplete
 - ▶ The possibility of adding optional information if present is an important feature
- ▶ Vocabulary with predefined semantics
- ▶ ...

Querying RDF: SPARQL

- ▶ SPARQL is the W3C recommendation query language for RDF (January 2008).
 - ▶ SPARQL is a recursive acronym that stands for *SPARQL Protocol and RDF Query Language*
- ▶ SPARQL is a graph-matching query language.
- ▶ A SPARQL query consists of three parts:
 - ▶ Pattern matching: optional, union, filtering, ...
 - ▶ Solution modifiers: projection, distinct, order, limit, offset, ...
 - ▶ Output part: construction of new triples,

SPARQL in a nutshell

```
SELECT ?Author
WHERE
{
  ?Paper      dc:creator      ?Author .
  ?Paper      dct:PartOf      ?Conf .
  ?Conf       swrc:series      conf: pods .
}
```

SPARQL in a nutshell

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A SPARQL query consists of a:

Body: Pattern matching expression

SPARQL in a nutshell

```
SELECT ?Author
WHERE
{
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}
```

A SPARQL query consists of a:

Body: Pattern matching expression

Head: Processing of the variables

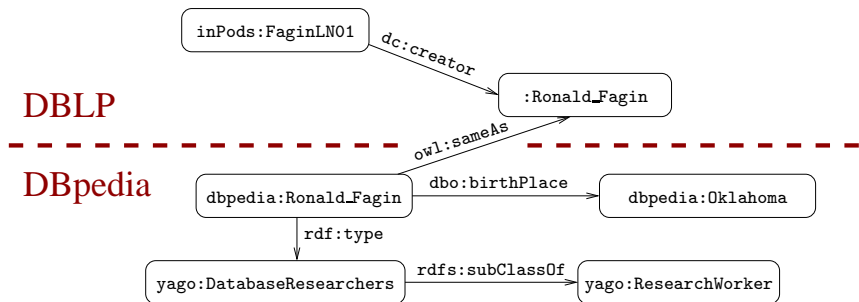
What are the challenges in implementing SPARQL?

SPARQL has to take into account the distinctive features of RDF:

- ▶ Should be able to extract information from interconnected RDF graphs
- ▶ Should be consistent with the open-world semantics of RDF
 - ▶ Should offer the possibility of adding optional information if present
- ▶ Should be able to properly interpret RDF graphs with a vocabulary with predefined semantics

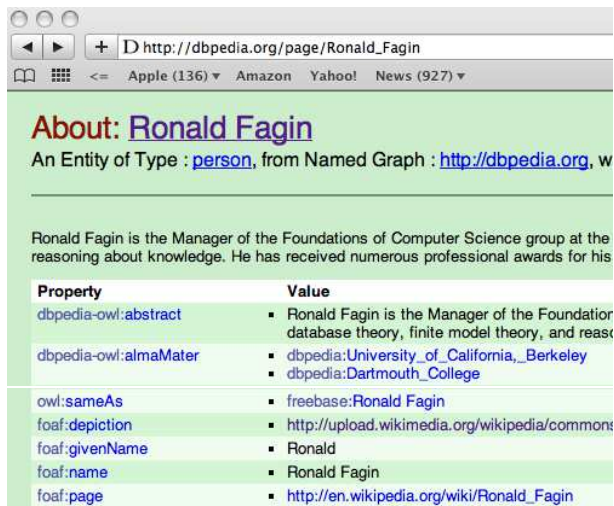
Extracting information from interconnected RDF graphs

```
      : <http://dblp.l3s.de/d2r/resource/authors/>
dbpedia: <http://dbpedia.org/resource/>
  rdf: <http://www.w3.org/1999/02/22-rdf-syntax-ns#>
  rdfs: <http://www.w3.org/2000/01/rdf-schema#>
  owl: <http://www.w3.org/2002/07/owl#>
yago: <http://dbpedia.org/class/yago/>
dbo: <http://dbpedia.org/ontology/>
```



Dereferenceable URIs are the glue

`http://dbpedia.org/resource/Ronald_Fagin`



The screenshot shows a web browser window with the address bar containing `http://dbpedia.org/page/Ronald_Fagin`. The page title is "About: [Ronald Fagin](#)". Below the title, it states "An Entity of Type : [person](#), from Named Graph : <http://dbpedia.org>, w".

Ronald Fagin is the Manager of the Foundations of Computer Science group at the reasoning about knowledge. He has received numerous professional awards for his

Property	Value
<code>dbpedia-owl:abstract</code>	<ul style="list-style-type: none">Ronald Fagin is the Manager of the Foundation database theory, finite model theory, and reaso
<code>dbpedia-owl:almaMater</code>	<ul style="list-style-type: none"><code>dbpedia:University_of_California,_Berkeley</code><code>dbpedia:Dartmouth_College</code>
<code>owl:sameAs</code>	<ul style="list-style-type: none"><code>freebase:Ronald Fagin</code>
<code>foaf:depiction</code>	<ul style="list-style-type: none">http://upload.wikimedia.org/wikipedia/commons
<code>foaf:givenName</code>	<ul style="list-style-type: none">Ronald
<code>foaf:name</code>	<ul style="list-style-type: none">Ronald Fagin
<code>foaf:page</code>	<ul style="list-style-type: none">http://en.wikipedia.org/wiki/Ronald_Fagin

Querying interconnected RDF graphs

Retrieve the authors that have published in PODS and were born in Oklahoma:

```
SELECT ?Author
WHERE
{
  ?Paper      dc:creator      ?Author .
  ?Paper      dct:PartOf      ?Conf .
  ?Conf       swrc:series      conf:pods .
  ?Person     owl:sameAs     ?Author .
  ?Person     dbo:birthPlace   dbpedia:Oklahoma .
}
```

Retrieving optional information

Retrieve the authors that have published in PODS, and their Web pages if this information is available:

```
SELECT ?Author ?WebPage
WHERE
{
  ?Paper      dc:creator      ?Author .
  ?Paper      dct:PartOf      ?Conf .
  ?Conf       swrc:series      conf:Pods .
  OPTIONAL { ?Author foaf:homePage ?WebPage . }
}
```

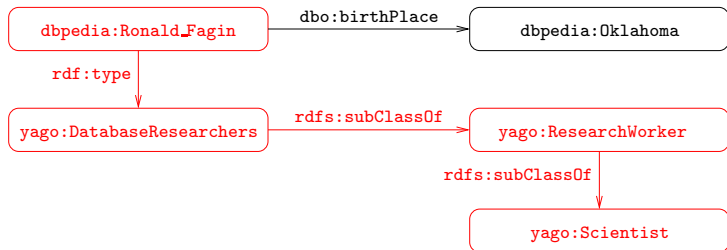
Taking into account vocabularies with predefined semantics

Retrieve the **scientists** that were born in Oklahoma and that have published in PODS:

```
SELECT ?Author
WHERE
{
  ?Author      rdf:type      yago:Scientist .
  ?Author      dbo:birthPlace dbpedia:Oklahoma .
  ?Paper       dc:creator    ?Author .
  ?Paper       dct:PartOf    ?Conf .
  ?Conf        swrc:series    conf:pods .
}
```

Taking into account vocabularies with predefined semantics

Retrieve the **scientists** that were born in Oklahoma and that have published in PODS:



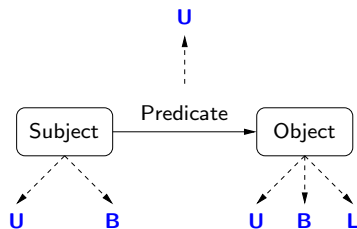
Outline of the talk

- ▶ RDF
- ▶ SPARQL: Syntax and semantics
- ▶ RDFS: RDF Schema
- ▶ Some new features in SPARQL 1.1
- ▶ Concluding remarks

Outline of the talk

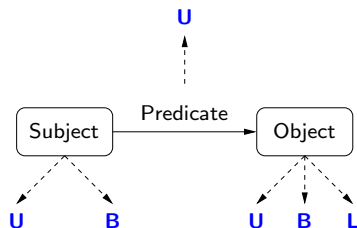
- ▶ **RDF**
- ▶ SPARQL: Syntax and semantics
- ▶ RDFS: RDF Schema
- ▶ Some new features in SPARQL 1.1
- ▶ Concluding remarks

RDF formal model



- U** : set of URIs
- B** : set of blank nodes
- L** : set of literals

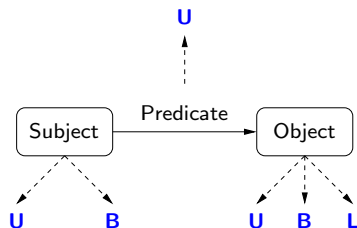
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$(s, p, o) \in (\mathbf{U} \cup \mathbf{B}) \times \mathbf{U} \times (\mathbf{U} \cup \mathbf{B} \cup \mathbf{L})$ is called an **RDF triple**

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$(s, p, o) \in (\mathbf{U} \cup \mathbf{B}) \times \mathbf{U} \times (\mathbf{U} \cup \mathbf{B} \cup \mathbf{L})$ is called an **RDF triple**

A set of RDF triples is called an **RDF graph**

Proviso

In this talk, we do not consider blank nodes

- ▶ $(s, p, o) \in \mathbf{U} \times \mathbf{U} \times (\mathbf{U} \cup \mathbf{L})$ is called an RDF triple

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SPARQL queries can be complex

Interesting features:

- ▶ Grouping
- ▶ Optional parts
- ▶ Nesting
- ▶ Union of patterns
- ▶ Filtering

```
{ P1  
  P2 }
```


SPARQL queries can be complex

Interesting features:

- ▶ **Grouping**
- ▶ Optional parts
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- ▶ Filtering

```
{ { P1  
  P2 }  
  
  { P3  
    P4 }  
  
}
```

SPARQL queries can be complex

Interesting features:

- ▶ Grouping
- ▶ **Optional parts**
- ▶ Nesting
- ▶ Union of patterns
- ▶ Filtering

```
{ { P1
  P2
  OPTIONAL { P5 } }

  { P3
    P4
    OPTIONAL { P7 } }

}
```

SPARQL queries can be complex

Interesting features:

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- ▶ Optional parts
- ▶ **Nesting**
- ▶ Union of patterns
- ▶ Filtering

```
{ { P1
  P2
  OPTIONAL { P5 } }

  { P3
    P4
    OPTIONAL { P7
      OPTIONAL { P8 } } }
}
```

SPARQL queries can be complex

Interesting features:

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- ▶ Optional parts
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- ▶ Filtering

```
{ { P1
  P2
  OPTIONAL { P5 } }

  { P3
    P4
    OPTIONAL { P7
      OPTIONAL { P8 } } }
}
```

UNION

```
{ P9 }
```

SPARQL queries can be complex

Interesting features:

- ▶ Grouping
- ▶ Optional parts
- ▶ Nesting
- ▶ Union of patterns
- ▶ **Filtering**

```
{ { P1
  P2
  OPTIONAL { P5 } }

  { P3
    P4
    OPTIONAL { P7
      OPTIONAL { P8 } } }
}
UNION
{ P9
  FILTER ( R ) }
```

SPARQL: An algebraic syntax

► Graph pattern:

`?X name ?Y`

$(?X, \text{name}, ?Y)$

`{ P1 . P2 }`

$(P_1 \text{ AND } P_2)$

`{ P1 OPTIONAL { P2 } }`

$(P_1 \text{ OPT } P_2)$

`{ P1 } UNION { P2 }`

$(P_1 \text{ UNION } P_2)$

`{ P1 FILTER (R) }`

$(P_1 \text{ FILTER } R)$

► SPARQL query:

`SELECT ?X ?Y ... { P }`

$(\text{SELECT } \{?X, ?Y, \dots\} P)$

SPARQL: An algebraic syntax (cont'd)

- ▶ **Explicit** precedence/association

Example

```
{ t1
  t2
  OPTIONAL { t3 }
  OPTIONAL { t4 }
  t5
}
```

$(((((t_1 \text{ AND } t_2) \text{ OPT } t_3) \text{ OPT } t_4) \text{ AND } t_5))$

Mappings: building block for the semantics

Definition

A mapping is a partial function:

$$\mu : \mathbf{V} \longrightarrow (\mathbf{U} \cup \mathbf{L})$$

The evaluation of a graph pattern results in a set of mappings.

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The evaluation of a graph pattern results in a set of mappings.

The semantics of triple patterns

Given an RDF graph G and a triple pattern t .

Definition

The evaluation of t over G is the set of mappings μ such that:

- ▶ μ has as domain the variables in t : $\text{dom}(\mu) = \text{var}(t)$
- ▶ μ makes t to match the graph: $\mu(t) \in G$

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Example

graph	triple	evaluation						
$(R_1, \text{name}, \text{john})$	$(?X, \text{name}, ?Y)$	<table border="1"><tr><td>μ_1:</td><td>R_1</td><td>john</td></tr><tr><td>μ_2:</td><td>R_2</td><td>paul</td></tr></table>	μ_1 :	R_1	john	μ_2 :	R_2	paul
μ_1 :			R_1	john				
μ_2 :			R_2	paul				
$(R_1, \text{email}, \text{J@ed.ex})$								
$(R_2, \text{name}, \text{paul})$								

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graph	triple	evaluation				
$(R_1, \text{name}, \text{john})$						
$(R_1, \text{email}, \text{J@ed.ex})$	$(?X, \text{name}, ?Y)$	μ_1 : <table border="1"><tr><td>?X</td><td>?Y</td></tr><tr><td>R_1</td><td>john</td></tr></table>	?X	?Y	R_1	john
?X	?Y					
R_1	john					
$(R_2, \text{name}, \text{paul})$		μ_2 : <table border="1"><tr><td>?X</td><td>?Y</td></tr><tr><td>R_2</td><td>paul</td></tr></table>	?X	?Y	R_2	paul
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R_1	john					
$(R_2, \text{name}, \text{paul})$		μ_2 : <table border="1"><tr><td>?X</td><td>?Y</td></tr><tr><td>R_2</td><td>paul</td></tr></table>	?X	?Y	R_2	paul
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R_2	paul					

Compatible mappings

Definition

Mappings μ_1 and μ_2 are compatible if they agree in their common variables:

If $?X \in \text{dom}(\mu_1) \cap \text{dom}(\mu_2)$, then $\mu_1(?X) = \mu_2(?X)$.

Example

	?X	?Y	?Z	?V
μ_1 :	R_1	john		
μ_2 :	R_1		J@edu.ex	
μ_3 :			P@edu.ex	R_2

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Example

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μ_1 :	R_1	john		
μ_2 :	R_1		J@edu.ex	
μ_3 :			P@edu.ex	R_2
$\mu_1 \cup \mu_2$:	R_1	john	J@edu.ex	

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μ_3 :			P@edu.ex	R_2
$\mu_1 \cup \mu_2$:	R_1	john	J@edu.ex	
$\mu_1 \cup \mu_3$:	R_1	john	P@edu.ex	R_2

Compatible mappings

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Example

	?X	?Y	?Z	?V
μ_1 :	R_1	john		
μ_2 :	R_1		J@edu.ex	
μ_3 :			P@edu.ex	R_2
$\mu_1 \cup \mu_2$:	R_1	john	J@edu.ex	
$\mu_1 \cup \mu_3$:	R_1	john	P@edu.ex	R_2

► μ_2 and μ_3 are not compatible

Sets of mappings and operations

Let Ω_1 and Ω_2 be sets of mappings.

Definition

Join: extends mappings in Ω_1 with compatible mappings in Ω_2

- ▶ $\Omega_1 \bowtie \Omega_2 = \{\mu_1 \cup \mu_2 \mid \mu_1 \in \Omega_1, \mu_2 \in \Omega_2 \text{ and } \mu_1, \mu_2 \text{ are compatible}\}$

Difference: selects mappings in Ω_1 that cannot be extended with mappings in Ω_2

- ▶ $\Omega_1 \setminus \Omega_2 = \{\mu_1 \in \Omega_1 \mid \text{there is no mapping in } \Omega_2 \text{ compatible with } \mu_1\}$

Definition

Union: includes mappings in Ω_1 and in Ω_2

$$\blacktriangleright \Omega_1 \cup \Omega_2 = \{\mu \mid \mu \in \Omega_1 \text{ or } \mu \in \Omega_2\}$$

Left Outer Join: extends mappings in Ω_1 with compatible mappings in Ω_2 **if possible**

$$\blacktriangleright \Omega_1 \bowtie \Omega_2 = (\Omega_1 \bowtie \Omega_2) \cup (\Omega_1 \setminus \Omega_2)$$

Given an RDF graph G .

Definition

$\llbracket t \rrbracket_G =$

$\llbracket (P_1 \text{ AND } P_2) \rrbracket_G =$

$\llbracket (P_1 \text{ UNION } P_2) \rrbracket_G =$

$\llbracket (P_1 \text{ OPT } P_2) \rrbracket_G =$

$\llbracket (\text{SELECT } W \text{ } P) \rrbracket_G =$

Given an RDF graph G .

Definition

$$\llbracket t \rrbracket_G = \{ \mu \mid \text{dom}(\mu) = \text{var}(t) \text{ and } \mu(t) \in G \}$$

$$\llbracket (P_1 \text{ AND } P_2) \rrbracket_G = \llbracket P_1 \rrbracket_G \bowtie \llbracket P_2 \rrbracket_G$$

$$\llbracket (P_1 \text{ UNION } P_2) \rrbracket_G = \llbracket P_1 \rrbracket_G \cup \llbracket P_2 \rrbracket_G$$

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$$\llbracket (\text{SELECT } W P) \rrbracket_G = \{ \mu|_W \mid \mu \in \llbracket P \rrbracket_G \}$$

Given an RDF graph G .

Definition

$$\llbracket t \rrbracket_G = \{ \mu \mid \text{dom}(\mu) = \text{var}(t) \text{ and } \mu(t) \in G \}$$

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$$\text{dom}(\mu|_W) = \text{dom}(\mu) \cap W \text{ and}$$

$$\mu|_W(?X) = \mu(?X) \text{ for every } ?X \in \text{dom}(\mu|_W)$$

Example

$(R_1, \text{name}, \text{john})$
 $(R_1, \text{email}, \text{J@ed.ex})$
 $(R_2, \text{name}, \text{paul})$

$((?X, \text{name}, ?Y) \text{ OPT } (?X, \text{email}, ?E))$

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Semantics of SPARQL: An example

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► from the **Join**

Semantics of SPARQL: An example

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► from the **Difference**

Semantics of SPARQL: An example

Example

$(R_1, \text{name}, \text{john})$
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R_1	john
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?X	?E
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► from the **Union**

Filter expressions (value constraints)

Filter expression: P FILTER R

- ▶ P is a graph pattern
- ▶ R is a built-in condition

We consider in R :

- ▶ equality = among variables and RDF terms
- ▶ unary predicate bound
- ▶ boolean combinations (\wedge , \vee , \neg)

Filter expressions (value constraints)

Example

Some filter expressions:

$$(?X = \text{conf: pods})$$
$$\neg(?X = \text{conf: pods})$$
$$(?X = \text{conf: pods}) \vee (?Y = \text{conf: sigmod})$$
$$(?X = \text{conf: pods}) \wedge \neg(?Y = \text{conf: sigmod})$$

Satisfaction of value constraints

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- ▶ R is $\neg R_1$ and $\mu \models R_1$ does not hold
- ▶ R is $(R_1 \vee R_2)$, and $\mu \models R_1$ or $\mu \models R_2$
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Definition

FILTER : selects mappings that satisfy a condition

$$\llbracket (P \text{ FILTER } R) \rrbracket_G = \{ \mu \in \llbracket P \rrbracket_G \mid \mu \models R \}$$

Outline of the talk

- ▶ RDF
- ▶ SPARQL: Syntax and semantics
- ▶ **RDFS: RDF Schema**
- ▶ Some new features in SPARQL 1.1
- ▶ Concluding remarks

Syntax of RDFS

RDFS extends RDF with a schema vocabulary: `subPropertyOf` (`rdf:sp`), `subClassOf` (`rdf:sc`), `domain` (`rdf:dom`), `range` (`rdf:range`), `type` (`rdf:type`).

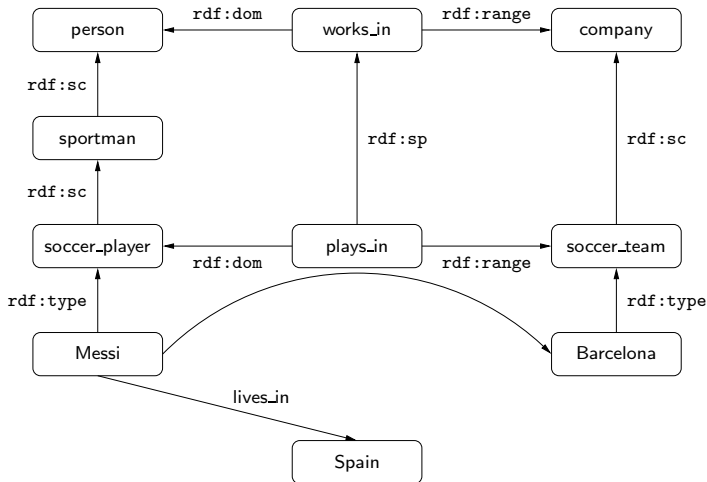
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How can one query RDFS data?

- ▶ Evaluating queries which involve this vocabulary is challenging

A simple SPARQL query: (Messi, rdf:type, person)



Checking whether a triple t is in a graph G is the basic step when answering queries over RDF.

- ▶ For the case of RDFS, we need to check whether t is implied by G

The notion of entailment in RDFS can be defined in terms of classical notions such as model, interpretation, etc.

- ▶ As for the case of first-order logic

This notion can also be characterized by a set of [inference rules](#).

An inference system for RDFS

Inference rule: $\frac{R}{R'}$

- ▶ R and R' are sequences of RDF triples including symbols \mathcal{A} , \mathcal{X} , ..., to be replaced by elements from $(\mathbf{U} \cup \mathbf{L})$

Instantiation of a rule: $\frac{\sigma(R)}{\sigma(R')}$

- ▶ $\sigma : \{\mathcal{A}, \mathcal{X}, \dots\} \rightarrow (\mathbf{U} \cup \mathbf{L})$

Application of a rule $\frac{R}{R'}$ to an RDF graph G :

- ▶ Select an assignment $\sigma : \{\mathcal{A}, \mathcal{X}, \dots\} \rightarrow (\mathbf{U} \cup \mathbf{L})$
- ▶ if $\sigma(R) \subseteq G$, then obtain $G \cup \sigma(R')$

An inference system for RDFS (cont'd)

Sub-property :
$$\frac{(\mathcal{A}, \text{rdf:sp}, \mathcal{B}) (\mathcal{B}, \text{rdf:sp}, \mathcal{C})}{(\mathcal{A}, \text{rdf:sp}, \mathcal{C})}$$

$$\frac{(\mathcal{A}, \text{rdf:sp}, \mathcal{B}) (\mathcal{X}, \mathcal{A}, \mathcal{Y})}{(\mathcal{X}, \mathcal{B}, \mathcal{Y})}$$

Subclass :
$$\frac{(\mathcal{A}, \text{rdf:sc}, \mathcal{B}) (\mathcal{B}, \text{rdf:sc}, \mathcal{C})}{(\mathcal{A}, \text{rdf:sc}, \mathcal{C})}$$

$$\frac{(\mathcal{A}, \text{rdf:sc}, \mathcal{B}) (\mathcal{X}, \text{rdf:type}, \mathcal{A})}{(\mathcal{X}, \text{rdf:type}, \mathcal{B})}$$

Typing :
$$\frac{(\mathcal{A}, \text{rdf:dom}, \mathcal{B}) (\mathcal{X}, \mathcal{A}, \mathcal{Y})}{(\mathcal{X}, \text{rdf:type}, \mathcal{B})}$$

$$\frac{(\mathcal{A}, \text{rdf:range}, \mathcal{B}) (\mathcal{X}, \mathcal{A}, \mathcal{Y})}{(\mathcal{Y}, \text{rdf:type}, \mathcal{B})}$$

The previous system of inference rules characterize the notion of entailment in RDFS (without blank nodes).

Thus, a triple t can be deduced from an RDF graph G ($G \models t$) if there exists an RDF G' such that:

- ▶ $t \in G'$
- ▶ G' can be obtained from G by successively applying the rules in the previous system.

Definition

The closure of an RDFS graph G ($\text{cl}(G)$) is the graph obtained by adding to G all the triples that are implied by G .

A basic property of the closure:

- ▶ $G \models t$ iff $t \in \text{cl}(G)$

Basic step for answering queries over RDFS:

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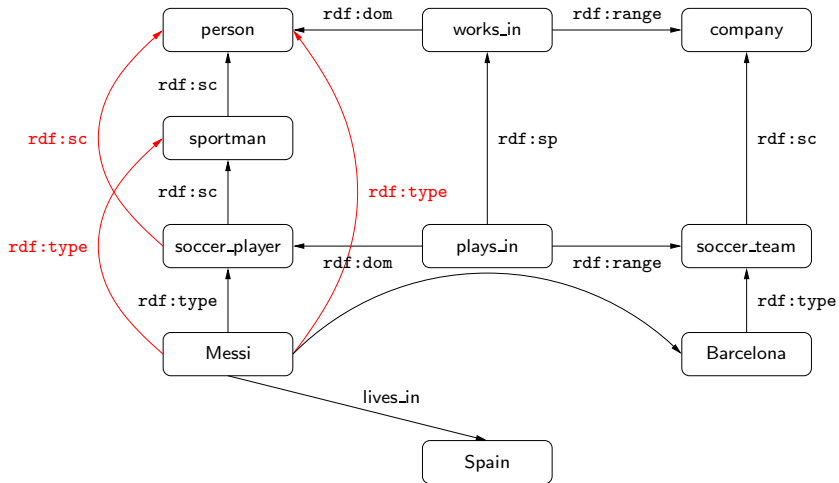
- ▶ Checking whether a triple t is in $cl(G)$

Definition

The *RDFS-evaluation* of a graph pattern P over an RDFS graph G is defined as the evaluation of P over $cl(G)$:

$$\llbracket P \rrbracket_G^{\text{rdfs}} = \llbracket P \rrbracket_{cl(G)}$$

Example: (Messi, rdf:type, person) over the closure



Answering SPARQL queries over RDFS

A simple approach for answering a SPARQL query P over an RDF graph G :

- ▶ Compute $cl(G)$, and then evaluate P over $cl(G)$ as for RDF

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- ▶ Once the closure has been computed, all the queries are evaluated over a graph which can be much larger than the original graph
- ▶ The approach is not goal-oriented

When evaluating $(a, \text{rdf:sc}, b)$, a goal-oriented approach should not compute $\text{cl}(G)$:

- ▶ It should just verify whether there exists a path from a to b in G where every edge has label rdf:sc

Extending SPARQL with navigational capabilities

The example $(a, \text{rdf:sc}, b)$ suggests that a query language with navigational capabilities could be appropriate for RDFS.

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This approach has some advantages:

- ▶ It is goal-oriented
- ▶ It has been used to design query languages for XML (e.g., XPath and XQuery). The results for these languages can be used here
- ▶ Navigational operators allow to express natural queries that are **not expressible in SPARQL over RDFS**

Outline of the talk

- ▶ RDF
- ▶ SPARQL: Syntax and semantics
- ▶ RDFS: RDF Schema
- ▶ Some new features in SPARQL 1.1
- ▶ Concluding remarks

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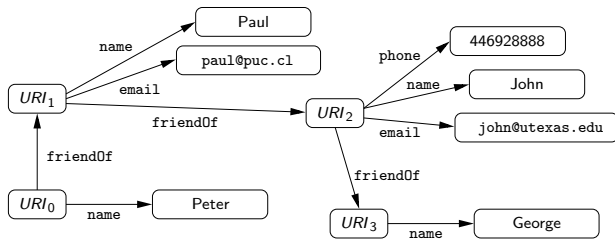
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Aggregates in SPARQL 1.1

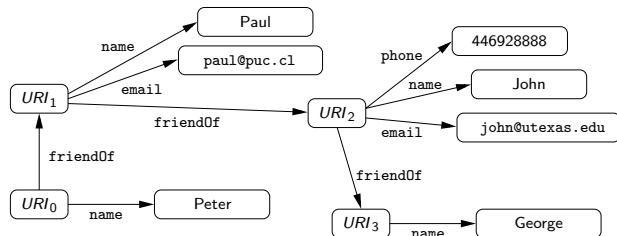
```
SELECT COUNT(DISTINCT ?Author)
WHERE
{
  ?Paper      dc:creator      ?Author .
  ?Paper      dct:PartOf      ?Conf .
  ?Conf       swrc:series      conf:Pods .
}
```

This query can be executed in the DBLP SPARQL endpoint.

SPARQL provides limited navigational capabilities

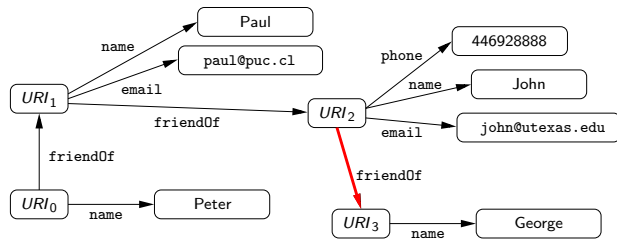


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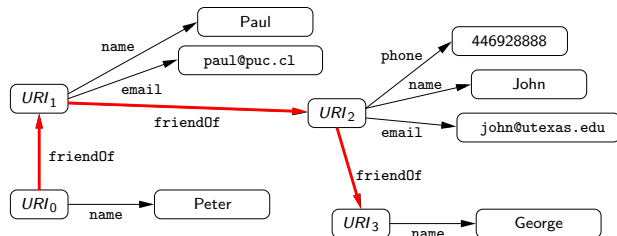
(SELECT ?X ((?X, friendOf, ?Y) AND (?Y, name, George)))

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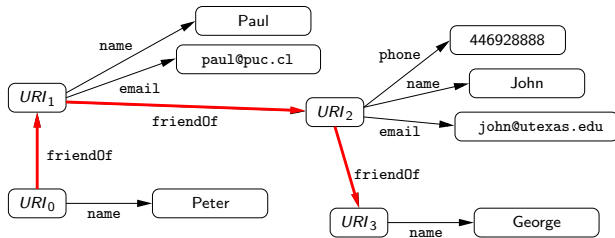
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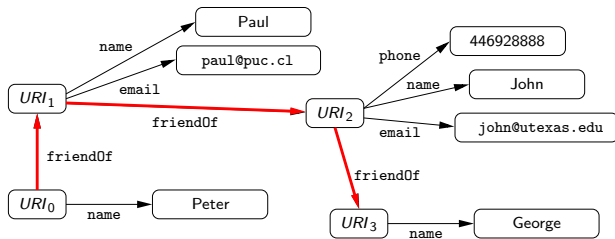


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A possible solution: Property paths



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(SELECT ?X ((?X, (friendOf)*, ?Y) AND (?Y, name, George)))

Navigational capabilities in SPARQL 1.1: Property paths

Syntax of property paths:

$$exp := a \mid exp/exp \mid exp|exp \mid exp^*$$

where $a \in \mathbf{U}$

Evaluating property paths

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Property paths in SPARQL 1.1

New element in SPARQL 1.1: A triple of the form (x, \textit{exp}, y)

- ▶ *exp* is a property path
- ▶ *x* (resp. *y*) is either an element from **U** or a variable

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Example

- ▶ $(?X, (rdf:sc)^*, ?Y)$: Verifies whether $?X$ is a subclass of $?Y$
- ▶ $(?X, (rdf:sp)^*, ?Y)$: Verifies whether $?X$ is a subproperty of $?Y$

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Example

- ▶ $(?X, \text{KLM}/(\text{KLM})^*, ?Y)$: It is possible to go from $?X$ to $?Y$ by using the airline KLM
- ▶ $((?X, \text{KLM}/(\text{KLM})^*, ?Y) \text{ FILTER } \neg(?X = ?Y))$: Same as before, but now $?X, ?Y$ must be different

SPARQL 1.1 and RDFS

Property paths can help in encoding the semantics of RDFS.

- ▶ Given a SPARQL graph pattern P , we would like to find a SPARQL 1.1 graph pattern Q such that:

$$\text{For every RDF graph } G: \llbracket P \rrbracket_G^{\text{rdfs}} = \llbracket Q \rrbracket_G$$

Property paths can help in encoding the semantics of RDFS.

- ▶ Given a SPARQL graph pattern P , we would like to find a SPARQL 1.1 graph pattern Q such that:

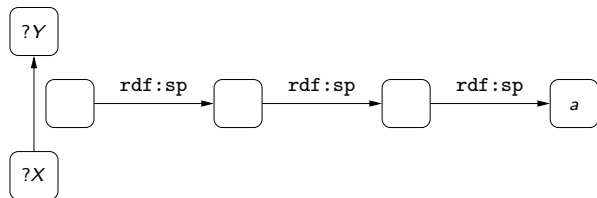
$$\text{For every RDF graph } G: \llbracket P \rrbracket_G^{\text{rdfs}} = \llbracket Q \rrbracket_G$$

We already saw how to encode `rdf:sc` and `rdf:sp`.

- ▶ We will consider the example $P = (?X, a, ?Y)$, where $a \in \mathbf{U} \setminus \{\text{rdf:sc}, \text{rdf:sp}, \text{rdf:type}, \text{rdf:dom}, \text{rdf:range}\}$

The case of $P = (?X, a, ?Y)$

What are the difficulties in this case?



The case of $P = (?X, a, ?Y)$ (cont'd)

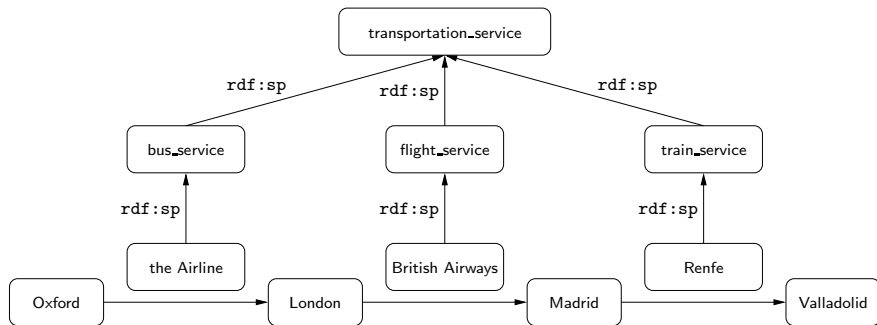
Let Q be:

$$\left(\text{SELECT } \{?X, ?Y\} \right. \\ \left. ((?X, ?Z, ?Y) \text{ AND } (?Z, (\text{rdf:sp})^*, a)) \right)$$

Then for every RDF graph G : $\llbracket P \rrbracket_G^{\text{rdfs}} = \llbracket Q \rrbracket_G$

Are we done?

List the pairs a, b of cities such that there is a way to travel from a to b .



Concluding remarks

- ▶ We have witnessed a constant growth in the amount of RDF data available on the Web
- ▶ Two fundamental components of the Semantic Web: RDF and SPARQL
- ▶ Some of the distinctive features of RDF have made the study and implementation of SPARQL challenging
- ▶ SPARQL is still under development: SPARQL 1.1, ...

Thank you!